


# Radiative transfer model in the generalized retrieval code “GRASP”

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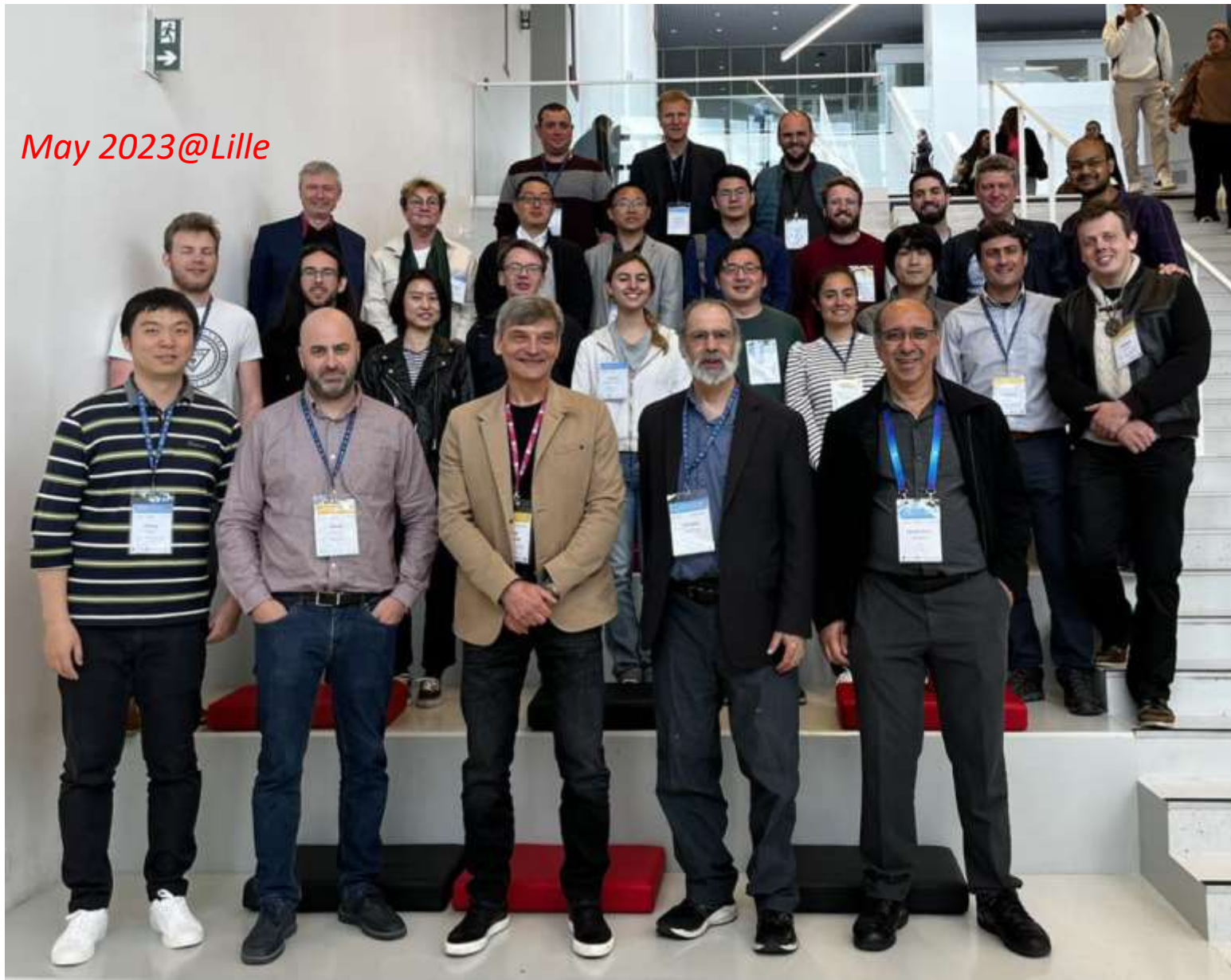
P. Litvinov, A. Lopatin, M. Herreras-Giralda,  
T. Lapyonok, O. Dubovik  
and  
 **GRASP** team



**GRASP** concept paper  
[Dubovik+21]

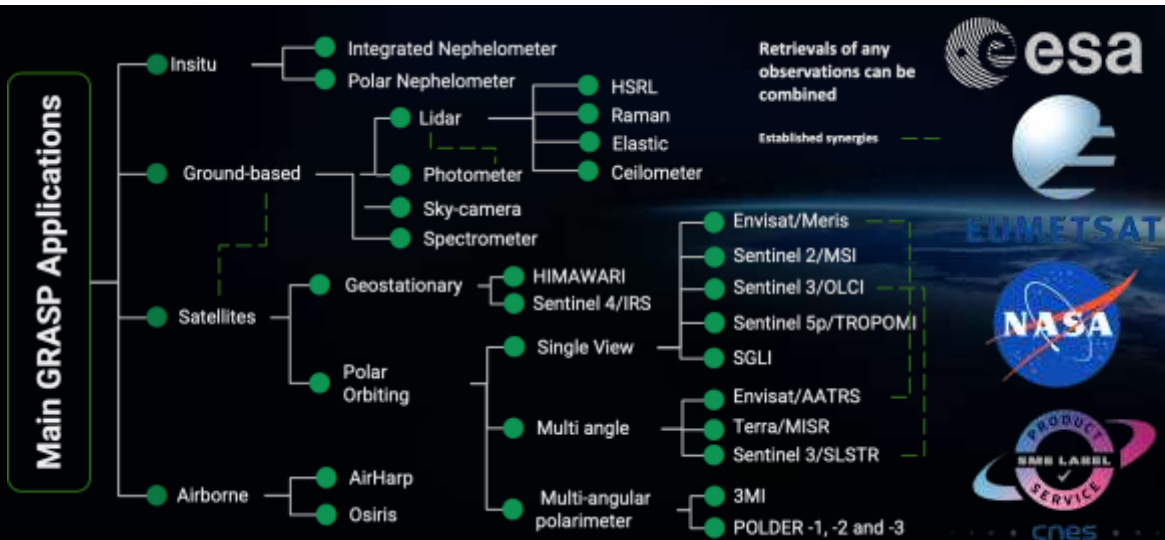
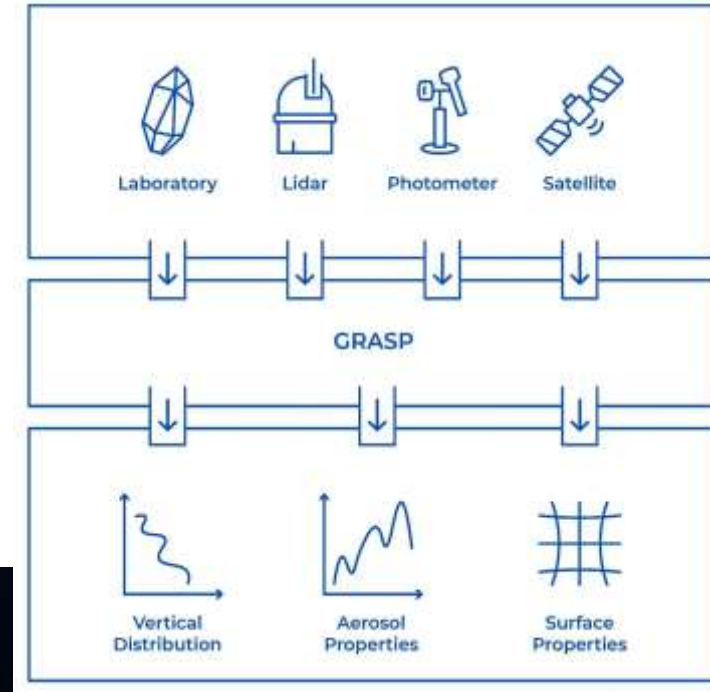


*May 2023@Lille*



**GRASP** stands for  
Generalized Retrieval of Atmosphere and Surface Properties

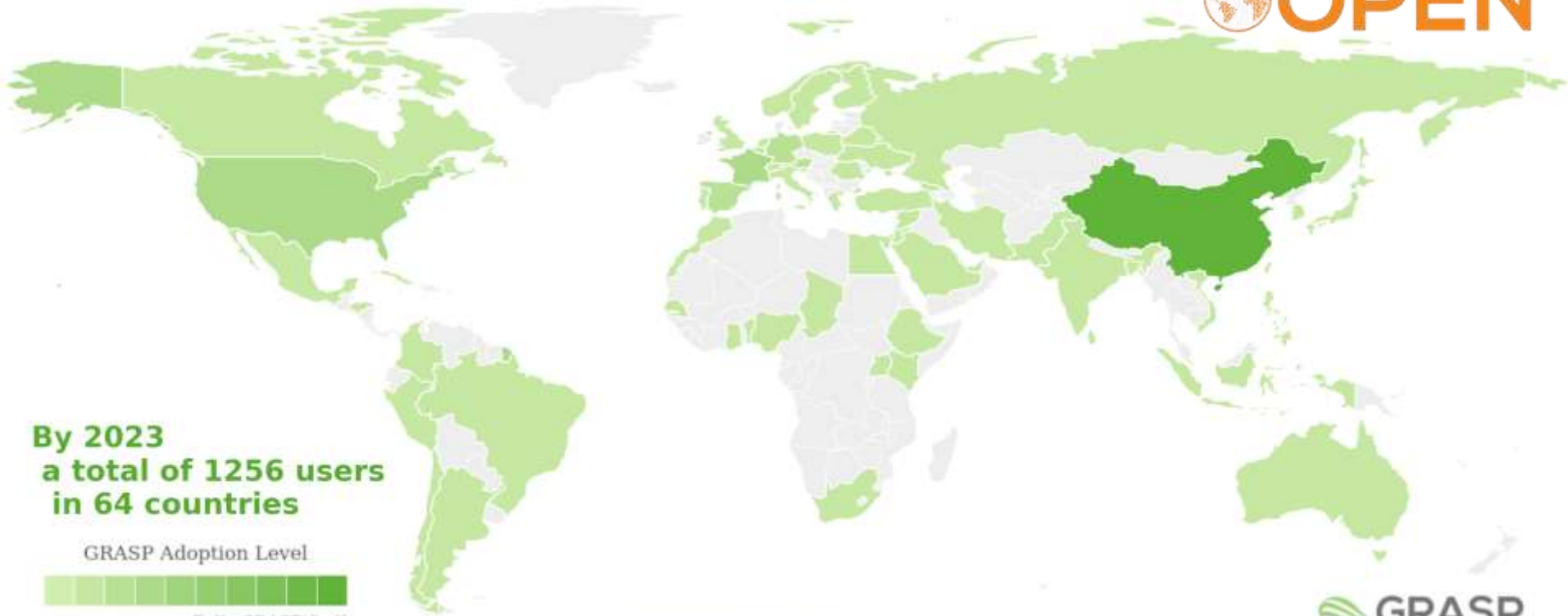
... is one of the most advanced algorithms for deriving aerosol, gas and surface properties. This inversion algorithm is currently used by space agencies worldwide for operational products. It was originally developed for use in AERONET sun-sky radiometers.



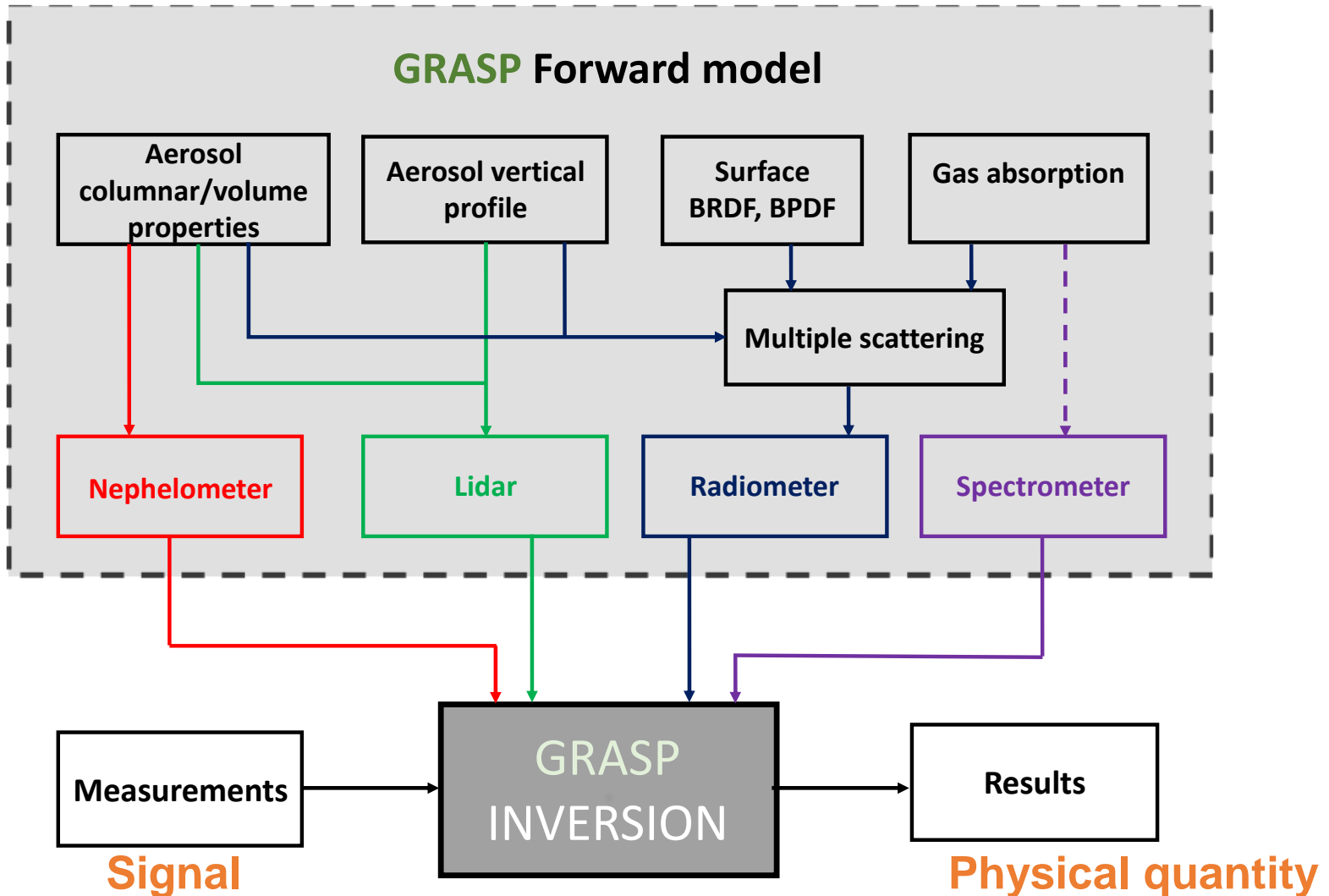
# GRASP community



**GRASP**  
 **OPEN**



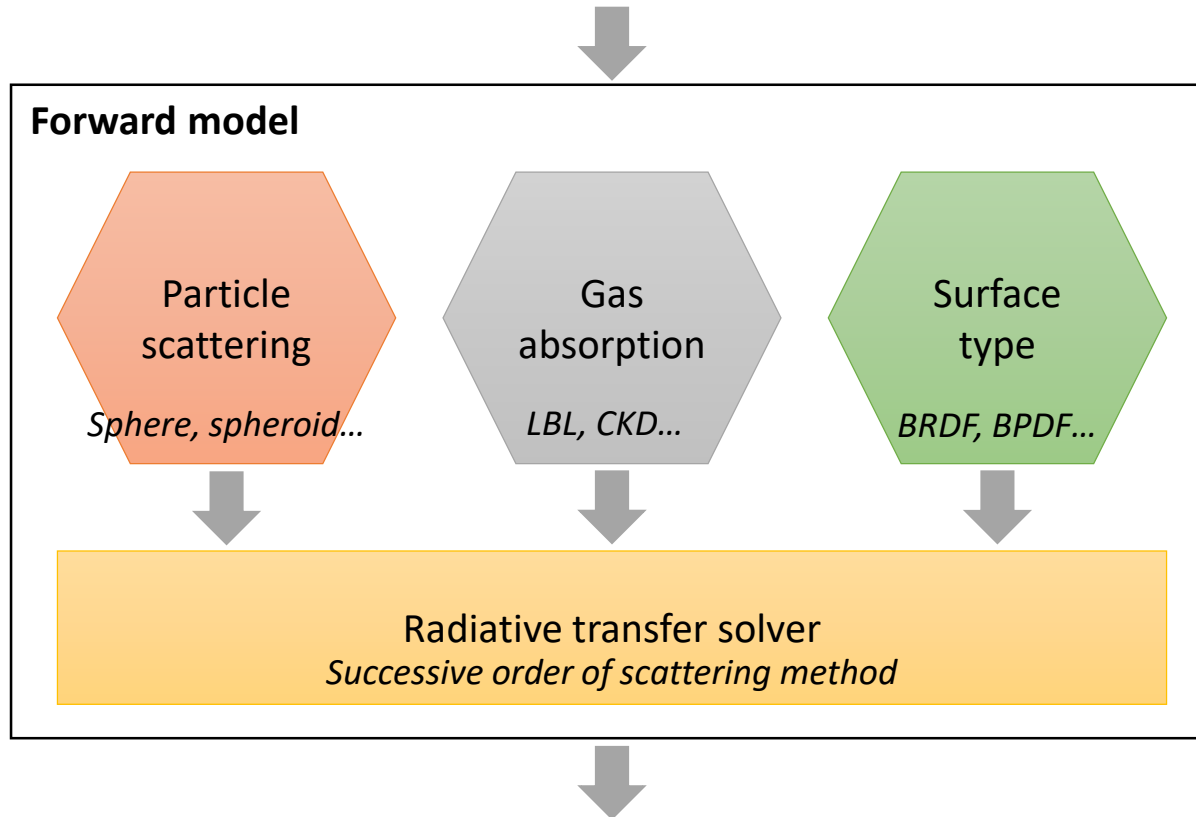
# General description of GRASP



# Radiative transfer model

*≈ forward model in remote sensing inversion*

**Physical quantities:** aerosol parameters, gas amount, surface conditions

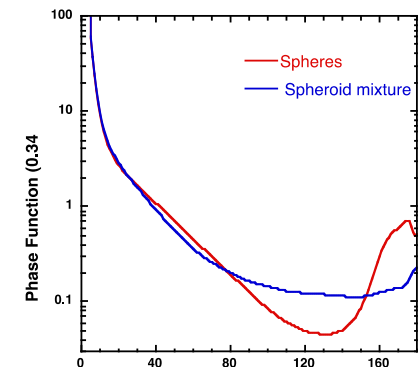
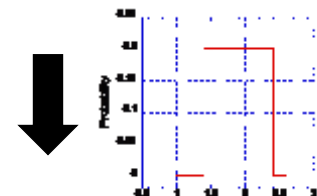
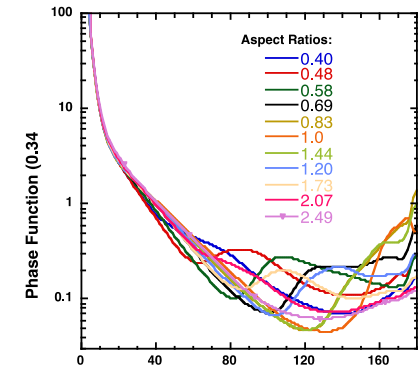
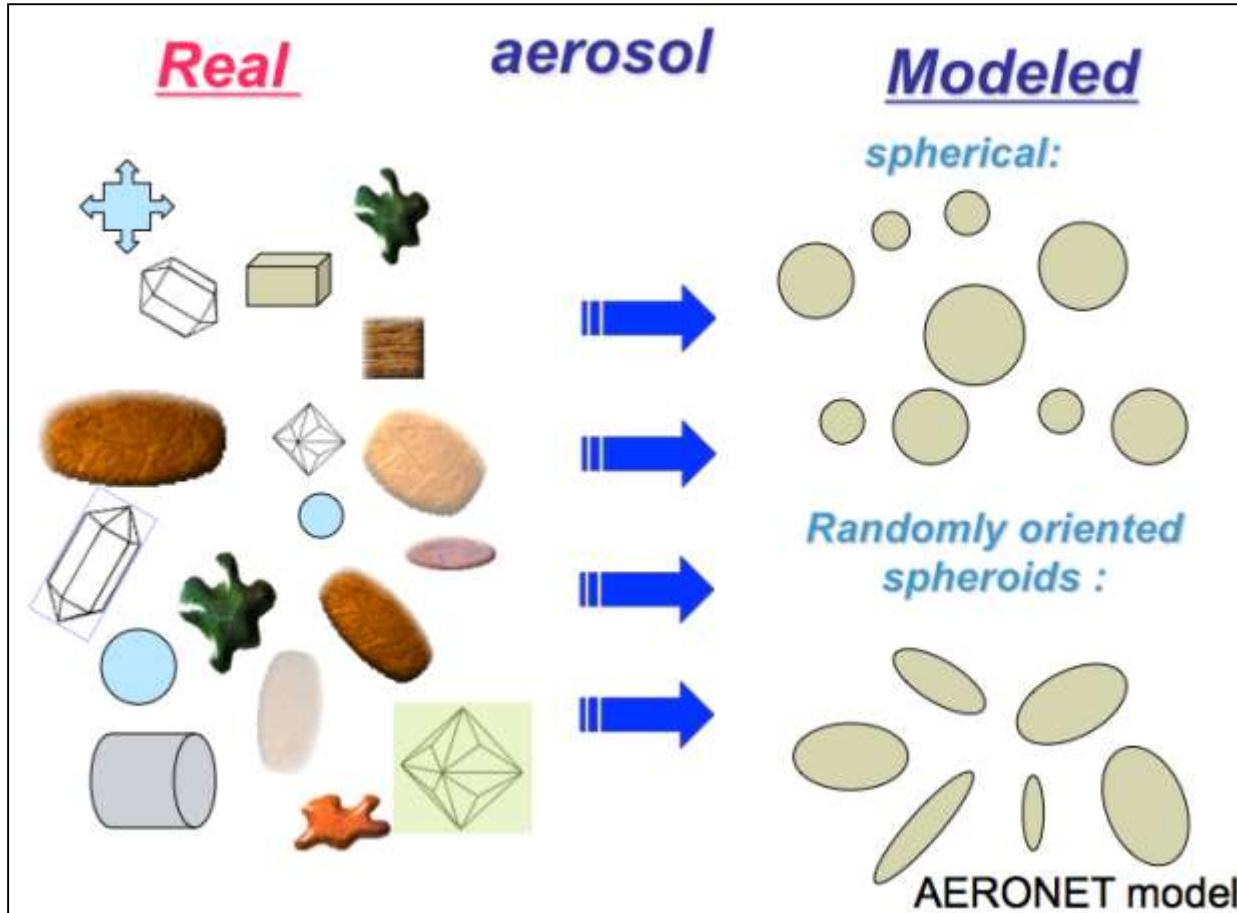


**Output:** radiance (reflectance), radiative flux, brightness temperature



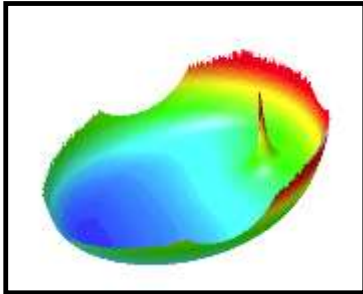
# Particle scatterings

Dubovik et al., 2006



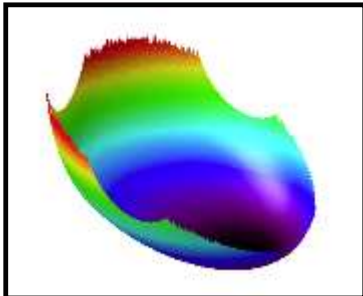
# Surface reflectance models

## BRDF



- (1) Rahman-Pity-Verstraete model (Rahman et al., 1993)
- (2) Ross-Li model (Ross, 1981; Li, X., Strahler, 1992)

## BRDF



- (1) One parametric BPDF (Maignan et al., 2009)
- (2) Fresnel facet model for Gaussian surfaces (Litvinov et al., 2011)

## BRDF+BPDF

**(Physically based models)**

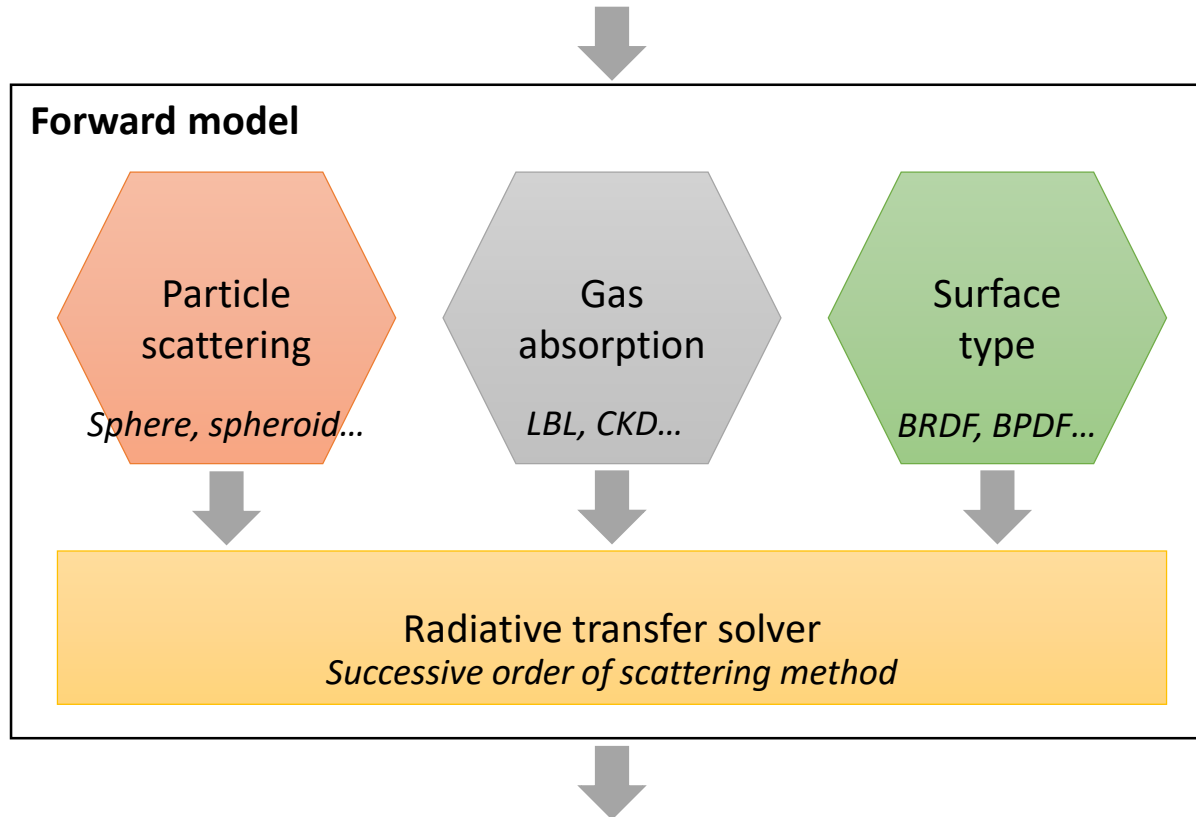
- (1) Cox-Munk ocean model
- (2) Land surface reflectance matrix (Litvinov et al., 2012)



# Radiative transfer model

*≈ forward model in remote sensing inversion*

**Physical quantities:** aerosol parameters, gas amount, surface conditions



**Output:** radiance (reflectance), radiative flux, brightness temperature



# Radiative transfer solver

Real scattering space

$$\mathbf{u} = \sum_{i=0}^{\infty} (2 - \delta_{m,0}) \mathbf{u}_m \cos[m(\phi - \phi_0)]$$


“Truncated” scattering space

$$\mathbf{u}^* = \sum_{i=0}^M (2 - \delta_{m,0}) \mathbf{u}_m^* \cos[m(\phi - \phi_0)]$$

“Forward lobe” scattering space

- Waquet & Herman (2019)
- Momoi et al. (2022)

Solution:

- Discrete ordinate method  
(e.g., Stamnes et al., Nakajima & Tanaka)
- **Successive order method:**  GRASP  
(e.g., Lenoble et al., Herreras-Giralda et al.)
- etc...

Idea:

$$\mu^* \frac{d\hat{\mathbf{u}}}{d\tau} = \mu^* \left[ \frac{d\mathbf{u}}{d\tau} - \frac{d\mathbf{u}^*}{d\tau} \right] =$$

$$-\hat{\mathbf{u}} + \hat{\omega} \int d\Omega \hat{\mathbf{P}}\hat{\mathbf{u}} + \hat{\omega} \hat{\mathbf{P}}\mathbf{F}_0 e^{-\frac{\tau}{\mu_0^*}} + \hat{\omega} \mathbf{O}_1 + \omega^* \mathbf{O}_2,$$

Waquet & Herman (2019)
P<sup>n</sup>IMS method  
Momoi et al. (2022ab)

Calculated radiance:  $\mathbf{u} \approx \hat{\mathbf{u}} + \mathbf{u}^*$

# RT solution under aerosol-laden atmosphere

⇒ Highly anisotropic aerosol phase function

○ Radiance :  $u = u^*$

○ Phase matrix :  $P(\Omega, \Omega') = P^*(\Omega, \Omega') + \hat{P}(\Omega, \Omega')$   
Truncated P Forward peak

●  $u^*$  : Numerical solution using spherical harmonics decomposition

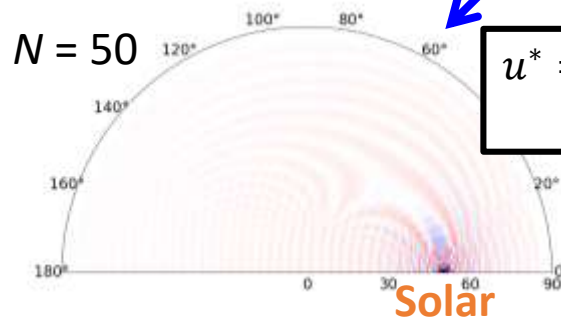
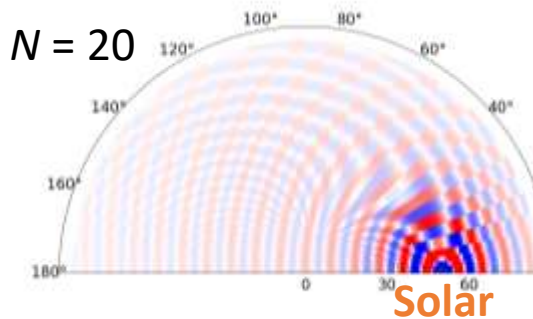
$$u^*(\tau^*, \Omega) = \sum_{m=0}^{M^*-1} u_m^*(\tau^*, \mu) \cos(m\phi)$$

Gaussian quadrature ( $N = M^*/2$ ) is used for solving.  
 ⇒ Computational time increases to  $N^{2-3}$  (e.g., DOM)

Reference radiance: Large  $N$  + ordinary single scattering correction (MS) method

- Aerosol laden atmosphere:  $N \sim 100$  (dust case)
- Cloud atmosphere:  $N \gg 100$

e.x.) dust aerosol case solved with  $\delta$ -M truncation



Forward peak generates Gibbs type angular oscillation

$$u^* = u_{\text{Ref}}[1 + \epsilon]$$

$u_{\text{Ref}}$  was given by  $N = 100$  with MS

10      0      -10 [%]

Difference  $\epsilon$

# Correction methods over a black surface

○ Radiance :  $u = u^* + \hat{u}$       ○ Phase matrix :  $P(\Omega, \Omega') = P^*(\Omega, \Omega') + \hat{P}(\Omega, \Omega')$   
Correction term      Truncated P      Forward peak

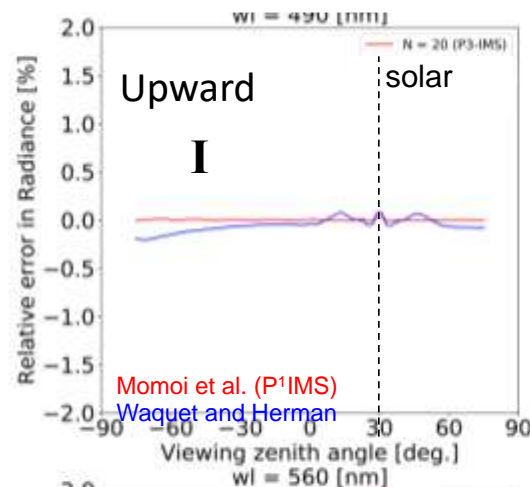
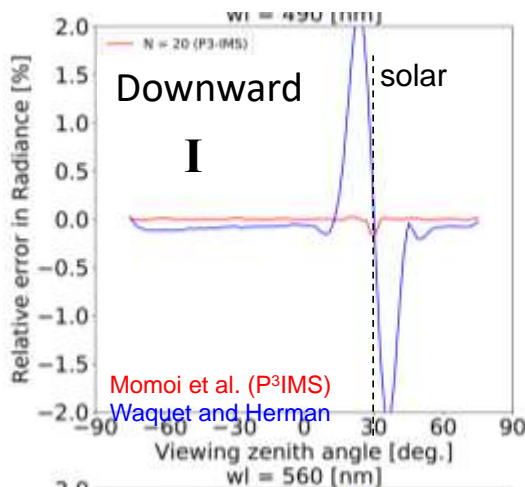
●  $u^*$  : Numerical solution using spherical harmonics decomposition

$$u^*(\tau^*, \Omega) = \sum_{m=0}^{M^*-1} u_m^*(\tau^*, \mu) \cos(m\phi) \rightarrow \text{Gaussian quadrature } (N = M^*/2) \text{ is used for solving.}$$

⇒ Computational time increases to  $N^{2\sim 3}$  (e.g., DOM)

●  $\hat{u}$  : Correction term solved perturbed RTE with a black surface by **successive order scattering**

$$\mu^* \frac{d\hat{u}(\tau, \Omega)}{d\tau} = \mu^* \left[ \frac{du(\tau, \Omega)}{d\tau} - \frac{du^*(\tau, \Omega)}{d\tau} \right] = \underbrace{-\hat{u} + \hat{\omega} \int d\Omega \hat{P} \hat{u} + \hat{\omega} \hat{P} F_0 e^{-\tau/\mu_0^*} + \hat{\omega} O_1 + \omega^* O_2}_{\text{Waquet and Herman (2019)}}$$



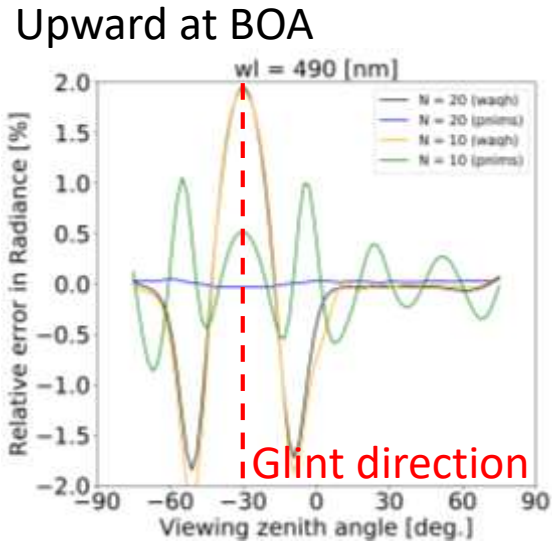
Waquet and Herman (2019)

P<sup>n</sup>IMS method

Nakajima and Tanaka (1988)

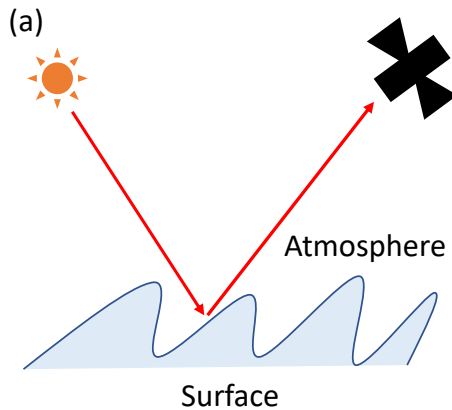
Momoi et al. (2022a)

Momoi et al. (2022b)

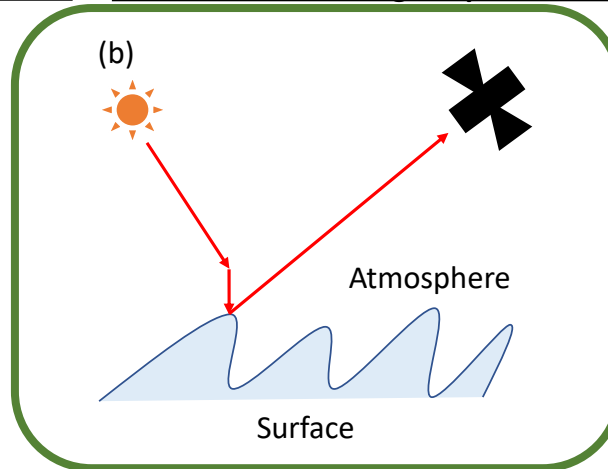


## What about sun-glint over ocean surface?

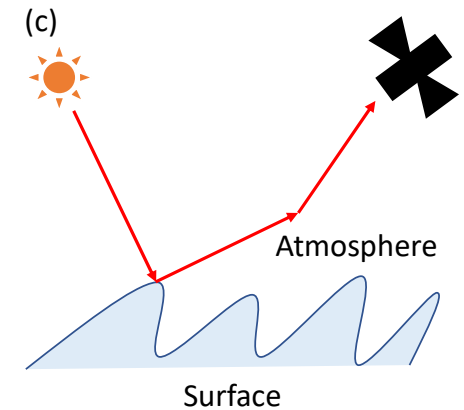
1<sup>st</sup> order of scattering in upward radiance



2<sup>nd</sup> order of scattering in upward radiance

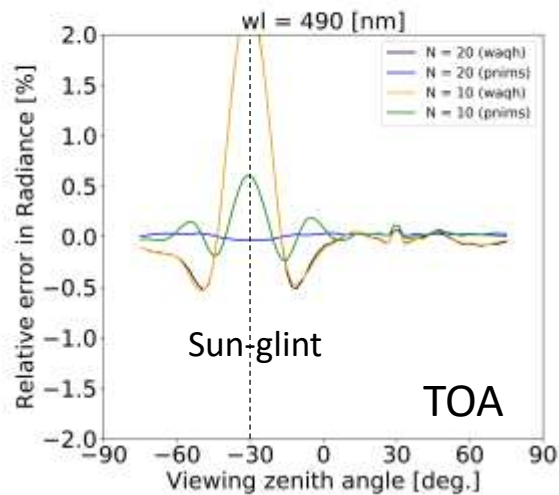


*P<sup>n</sup>IMS w/ sun-glint correction*

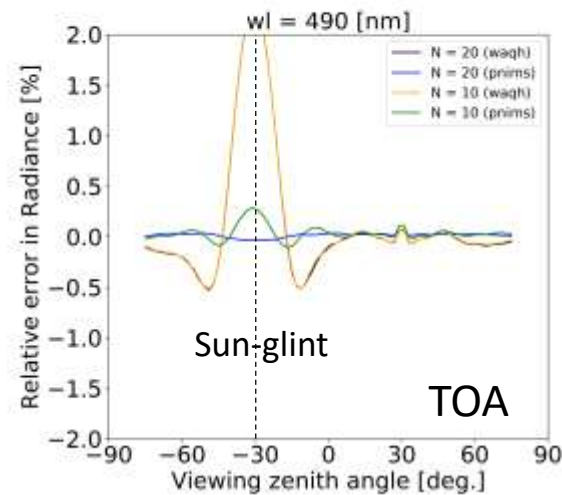


# Sun-glint correction using P<sup>n</sup>IMS method

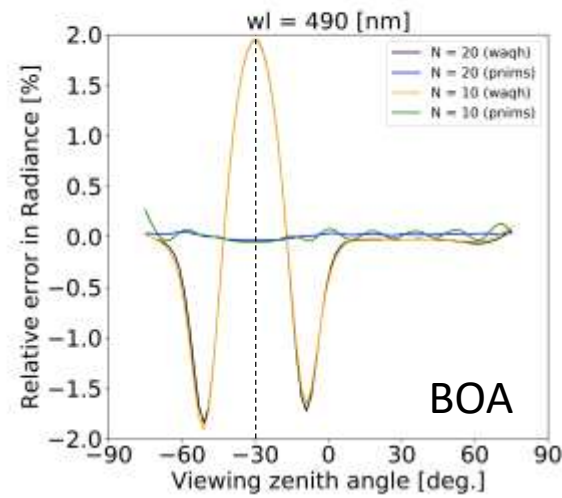
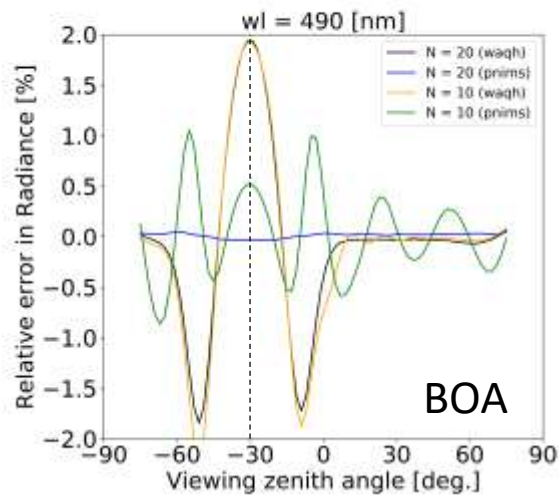
P<sup>n</sup>IMS w/o sun-glint correction



P<sup>n</sup>IMS w/ sun-glint correction



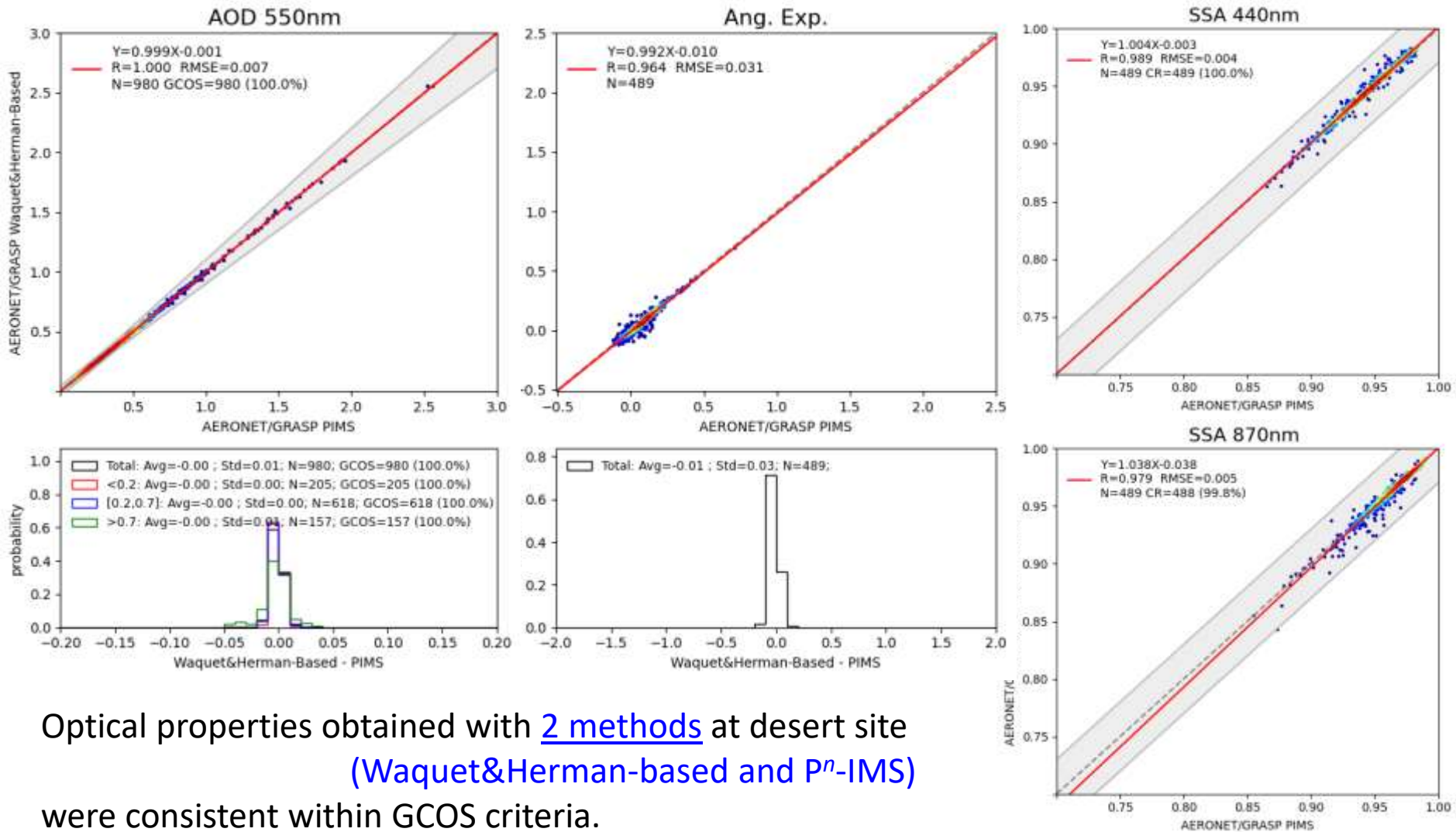
Waquet-Herman  
P<sup>n</sup>IMS-method





# Preliminary: AERONET, Banizoumbou, 2008

Fourier truncation order  $M = 10$

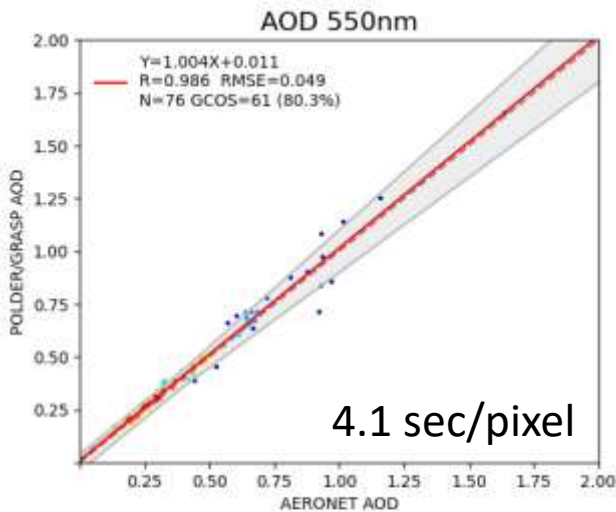


Optical properties obtained with [2 methods](#) at desert site  
(Waquet&Herman-based and  $P^n$ -IMS)  
were consistent within GCOS criteria.

# Preliminary: POLDER, Abu\_Al\_Bukhoosh, 2008

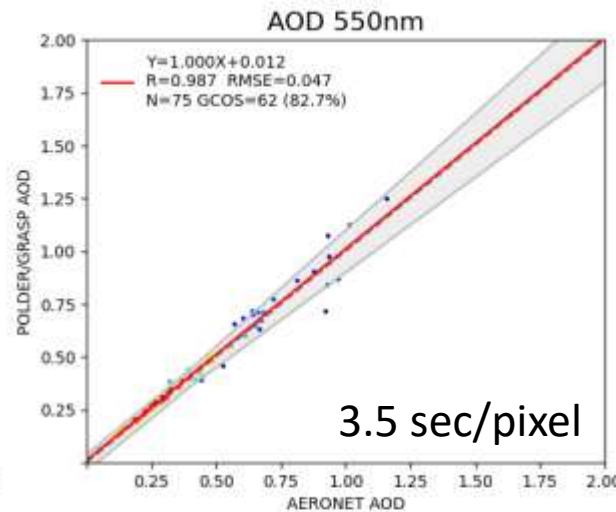
Fourier truncation order  $M = 7$

Waquet-Herman



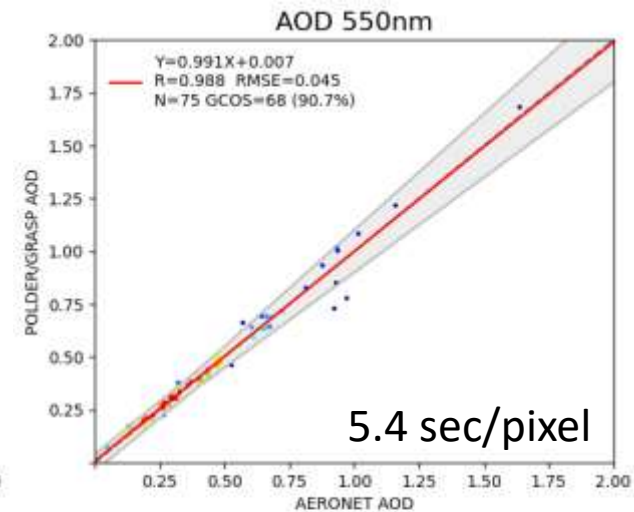
4.1 sec/pixel

$P^n$ IMS w/o glint cor.

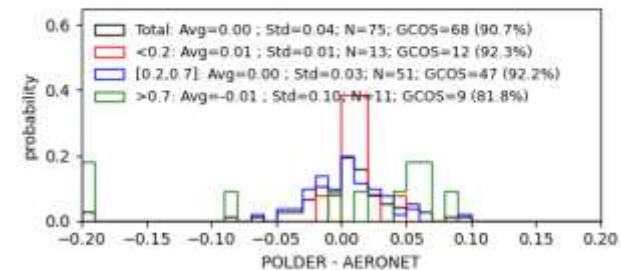
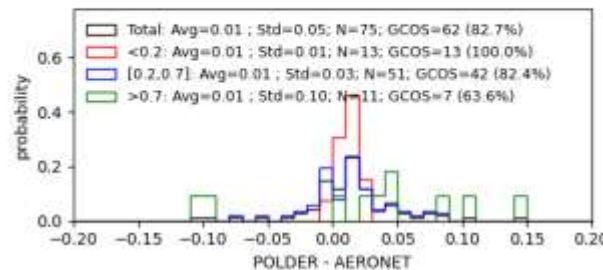
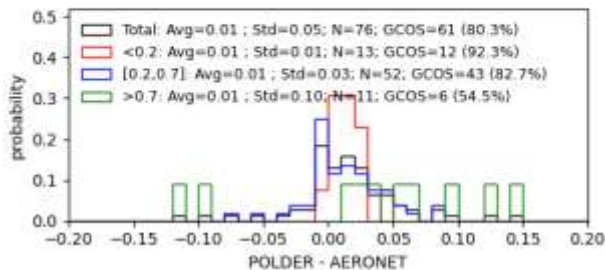


3.5 sec/pixel

$P^n$ IMS w/ glint cor.



5.4 sec/pixel



“ $P^n$ IMS w/ glint cor.” improved R, RMSE, N. of GCOS criteria.

The speed is  $P^n$ IMS w/o glint < Waquet-Herman <  $P^n$ IMS w/ glint << w/ glint truncation ( $P^n$ IMS  $M = 20$ )

# Join us!



**GRASP**  
 **OPEN**

